Completions of upper-triangular matrices to Kato nonsingularity

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In this paper we consider the problem of completion of the uppertriangular operator matrix $\begin{bmatrix} A & ? \\ 0 & B \end{bmatrix}$, where $A \in \mathcal{B}(\mathcal{H})$ and $B \in \mathcal{B}(\mathcal{K})$, to Kato nonsingular operators and completely solve it in each of the following cases: one of the operators A or B is Kato nonsingular; B is injective; A is with dense range; B is with finite ascent; A is with finite descent; $0 \notin int(\sigma_p(B))$; $0 \notin int(\sigma_{cp}(A))$. In particular, the results generalize and complete some of the previously obtained concerning the same problem.

This is a joint work with D. S. Cvetković-Ilić.